

$$1) \quad (x, \sin x) \quad (x+h, \sin(x+h))$$

$$x_1 \quad y_1 \quad x_2 \quad y_2$$

$$\begin{aligned} \frac{d(\sin x)}{dx} &= \frac{\sin(x+h) - \sin x}{x+h - x} \\ &= \frac{\sin(x+h) - \sin x}{h} \\ &= \frac{\sin x \cosh h + \cos x \sinh h - \sin x}{h} \\ &= \frac{\sin x \cosh h - \sin x}{h} + \frac{\cos x \sinh h}{h} \\ &= \left( \frac{\cosh h - 1}{h} \right) \sin x + \left( \frac{\sinh h}{h} \right) \cos x \end{aligned}$$

As  $h \rightarrow 0$

$$\begin{aligned} \frac{d(\sin x)}{dx} &= (0) \sin x + (1) \cos x \\ &= \underline{\cos x} \end{aligned}$$

$$2) \quad (x, \cos x) \quad (x+h, \cos(x+h))$$

$$x_1 \quad y_1 \quad x_2 \quad y_2$$

$$\begin{aligned} \frac{d(\cos x)}{dx} &= \frac{\cos(x+h) - \cos x}{x+h - x} \\ &= \frac{\cos x \cosh h - \sin x \sinh h - \cos x}{h} \\ &= \frac{\cos x \cosh h - \cos x}{h} - \frac{\sin x \sinh h}{h} \\ &= \left( \frac{\cosh h - 1}{h} \right) \cos x - \left( \frac{\sinh h}{h} \right) \sin x \end{aligned}$$

As  $h \rightarrow 0$

$$\begin{aligned} \frac{d(\cos x)}{dx} &= (0) \cos x - (1) \sin x \\ &= \underline{\underline{-\sin x}} \end{aligned}$$