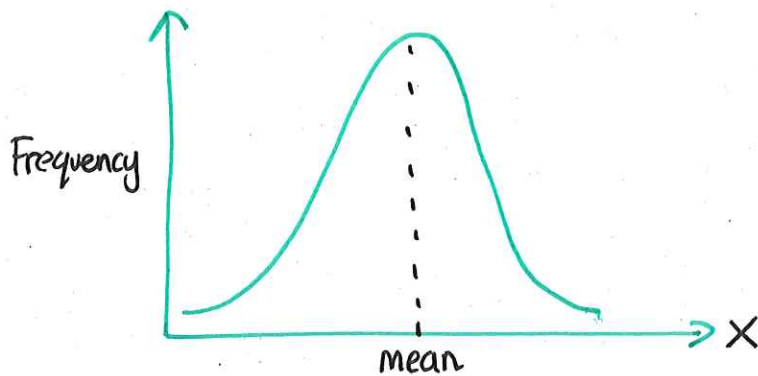


YEAR 2 APPLIED CHAPTER 3 — NORMAL DISTRIBUTION

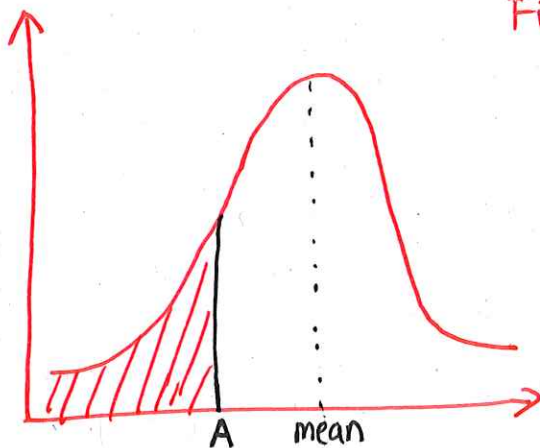
NORMAL DISTRIBUTION



$$X \sim N(\text{mean}, \text{variance})$$

$$X \sim N(\mu, \sigma^2)$$

NORMAL CD



Find $P(X < A) =$

NORMAL CD

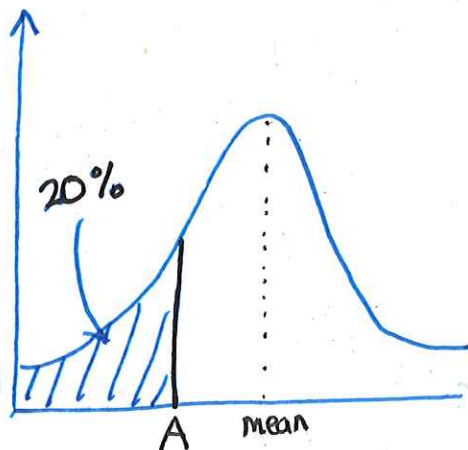
Lower : -100000 !

Upper : A

μ : mean

σ : standard deviation

INVERSE NORMAL



Find A

inverse normal

Area : 0.2

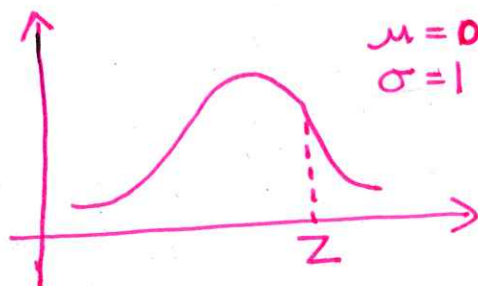
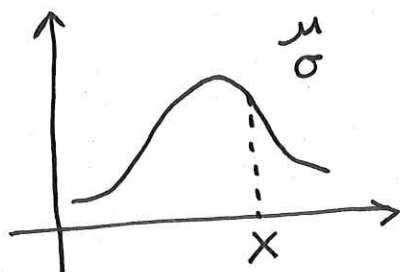
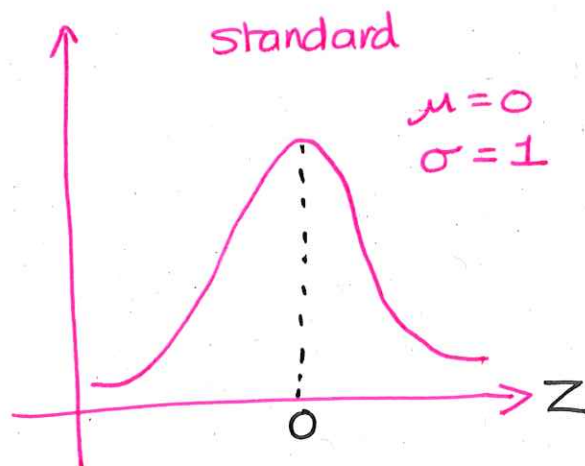
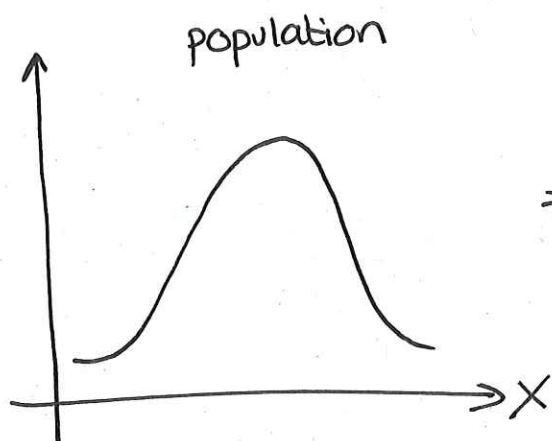
σ : standard deviation

μ : mean

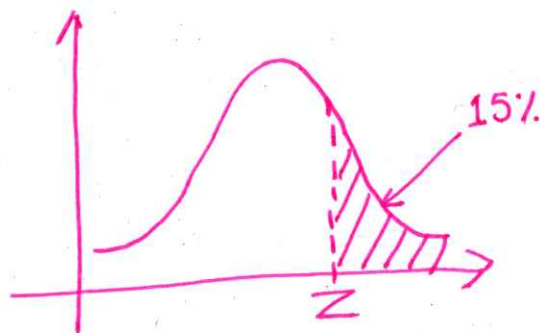
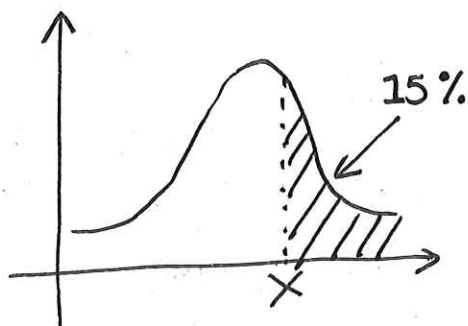
STANDARD NORMAL

convert population distribution to standard distribution.

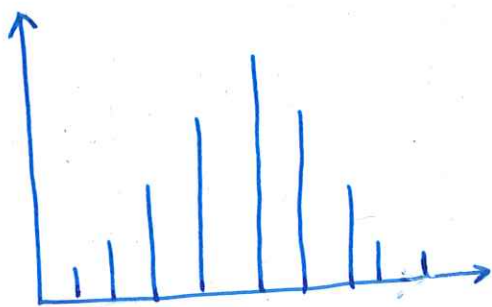
why? because standard distribution has know mean ($\mu=0$) and standard deviation ($\sigma=1$) values



$$Z = \frac{X - \mu}{\sigma}$$



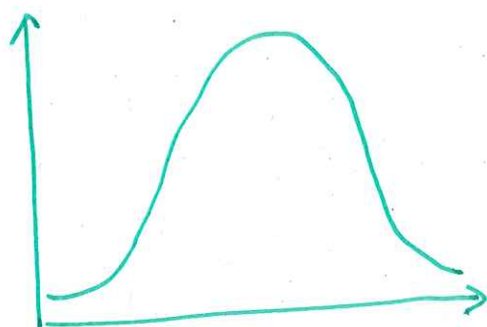
APPROXIMATING BINOMIAL DISTRIBUTION



BINOMIAL DISTRIBUTION

$$X \sim B(\text{number of trials}, \text{probability of success})$$

$$X \sim B(n, p)$$

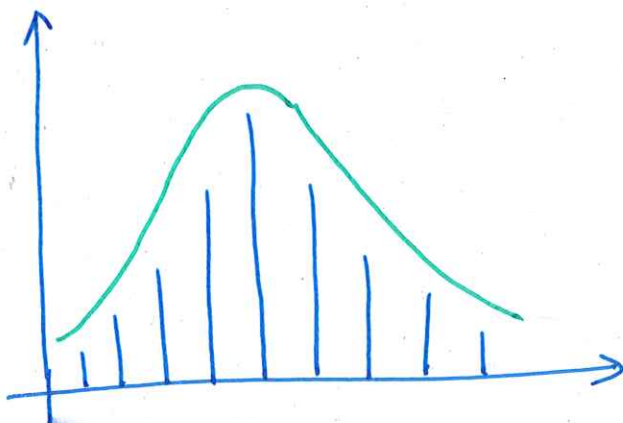


NORMAL DISTRIBUTION

$$X \sim N(\text{mean}, \text{variance})$$

$$X \sim N(\mu, \sigma^2)$$

If n is large and p is close to 0.5 then binomial distribution can be approximated by normal distribution



$$X \sim B(n, p)$$

$$Y \sim N(np, \sqrt{np(1-p)^2})$$

$$\text{mean} = np$$

$$\text{Standard Deviation} = \sqrt{np(1-p)}$$

Continuity Correction

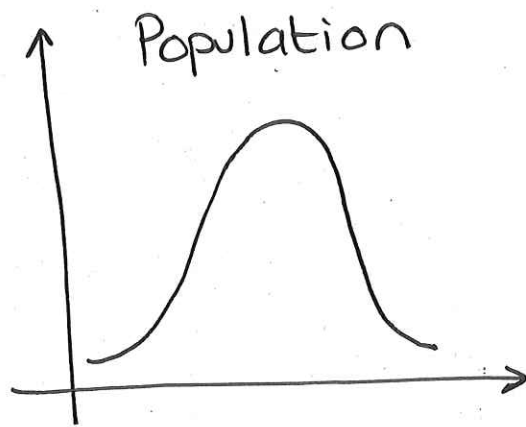
Discrete

$$X = 30$$

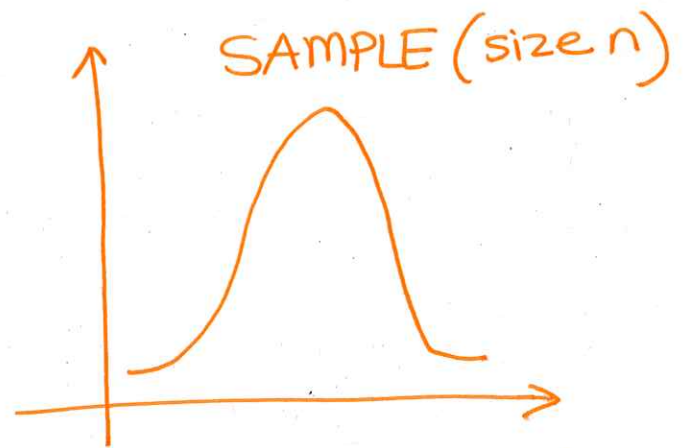
Continuous

$$29.5 \leq Y < 30.5$$

HYPOTHESIS TESTING ON SAMPLE MEAN



$$X \sim N(\mu, \sigma)$$



$$X \sim N\left(\mu, \sqrt{\frac{\sigma^2}{n}}\right)$$

mean = μ (of population)

$$SD = \sqrt{\frac{\sigma^2}{n}}$$

- Step 1. State your hypotheses
- Step 2. State your distribution for the sample
- Step 3. Calculate the probability of your sample happening (using sample normal distribution)
- Step 4. Compare probability with the significant level
- Step 5. Accept or Reject your H_0